



Proof of Goldbach Conjecture

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ABSTRACT

Goldbach conjecture states that every positive even integer can be expressed as the sum of two prime numbers. Basic concepts of number theory are used to prove this conjecture.

KEYWORDS: prime, odd, even

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Proof

Let x and y be two non-prime odd numbers and z be any even number.

Now,

every odd number can be expressed as the sum of two even numbers,

Therefore,

$$x+y=z$$

Let k be the common factor of x and y .

k is odd (since x and y are odd)

Therefore,

$$k(x'+y')=z$$

$\Rightarrow x'+y'=m$ (since k is a factor of z)

m is even (since $\text{even} \div \text{odd} = \text{even}$)

Now x' and y' are prime numbers and m is even.

Hence, every even number can be expressed as the sum of two prime numbers.

Reference

Wikipedia

